# Laterally Electrostatically Driven Poly 3C-SiC Folded-Beam Resonant Microstructures\*

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**Abstract:** Micromachined comb-drive electrostatic resonators with folded-cantilever beams were designed and fabricated. A combination of Rayleigh's method and finite-element analysis was used to calculate the resonant frequency drift as we adjusted the device geometry and material parameters. Three micromachined lateral resonant resonators with different beam widths were fabricated. Their resonant frequencies were experimentally measured to be 64.5,147.2, and 255.5kHz, respectively, which are in good agreement with the simulated resonant frequency. It is shown that an improved frequency performance could be obtained on the poly 3C-SiC based device structural material systems with high Young's modulus.

Key words: lateral resonant device; folded-beam; comb structure; MEMS; resonator; silicon carbide EEACC: 2575

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# 1 Introduction

Micromachined resonators are emerging as potential on-chip replacements for conventional discrete oscillators and filters in high performance communication transceivers. Electrostatic excitation combined with capacitive (electrostatic) detection is an attractive approach for silicon microstructures because of its simplicity and compatibility with micromachining technology<sup>[1]</sup>. SiC is a wide band gap semiconductor material well known for its mechanical characteristics, such as high Young's modulus and chemical inertness, yield strength, high thermal conductivity, and electrical stability at temperatures well above  $600\,{\rm \mathring{C}}\,{}^{[2]}$  . The first two properties in particular make it an excellent material to fabricate high frequency and high quality factor MEMS devices. Several groups have reported the fabrication methods of MEMS and NEMS resonators. They used polysilicon<sup>[3]</sup>, poly- $SiC^{[4]}$ , and monocrystalline  $3C-SiC^{[5]}$  as the structure materials.

In this paper, we describe the design, fabrication, and initial testing of an electrostatic comb structure for exciting and sensing the vibration of poly 3C-SiC microstructures parallel to the plane of the substrate. A combination of Rayleigh's method and finiteelement analysis is used to calculate the device resonant frequency as we adjust the device geometry and material parameters.

## 2 Theory and design

### 2.1 Electrostatic comb drive

Figure 1 shows the layout of a linear resonant structure that can be driven electrostatically from one side and sensed capacitively at the other side with interdigitated finger (comb) structures. If a capacitor is charged so that a voltage difference of V appears between its electrodes, the exerted electrostatic force on the electrodes,  $F_V$ , is found from:

$$F_{\rm v} = \nabla W = \frac{V^2}{2} \nabla C \tag{1}$$



Fig.1 (a) Layout of the linear resonant structure; (b) Enlarged view of the linear comb structure

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First mode Second mode Third mode

Fig. 2 Vibrating modes of the folded-beam resonators Arrows indicate direction of vibration.

For force components along the x-direction, as shown in Fig. 1, we have:

$$F_x = -\frac{V^2}{2} \times \frac{\partial}{\partial x} \left( \frac{\varepsilon_0 xt}{d} \right) = -\frac{\varepsilon_0 t}{2d} V^2$$
(2)

where  $\varepsilon_0$  is the dielectric constant, d is the gap between the plates, and t is the thickness of the plate. In Eq. (2),  $-\frac{\varepsilon_0 t}{2d}$  is a constant, which is independent of the lateral displacement (x) when x is less than the finger overlap (Fig. 1). Therefore, electrostatic-comb drives can have linear electromechanical transfer functions for large displacements, in contrast to parallel-plate capacitive drives.

### 2.2 Resonant structure design

Motions for these trusses suspension are capable of relief of the built-in residual strain in the structural film. Both the average residual stress in the poly 3C-SiC film and the stress induced by large-amplitude plate motion should be largely relieved by this design<sup>[6]</sup>. In addition, the long effective support lengths result in a highly compliant suspension. Plates with a  $100\mu$ m-long folded-beam resonate with amplitudes as large as  $5\mu$ m.

Figure 2 illustrates the first three vibrating modes of the folded-beam resonator. In the first mode, the vibrating direction is vertical to the plate plane. The second mode is a torsional resonant form. The third mode is in-plane vibration. Because of electrostatic restriction, the resonator only works in the third mode.

In the third in-plane vibrating mode, the trusses of the folded-beam displace at half the velocity of the plate (seen in Fig. 3) and the displacements distributing along the beam length direction are given by Ref. [7].

$$x_{1}(y) = \frac{x_{0}}{2} \left[ 3 \left( \frac{y}{L} \right)^{2} - 2 \left( \frac{y}{L} \right)^{3} \right]$$
$$x_{2}(y) = x_{0} - x_{t}(y)$$
(3)

where  $x_0$  is the maximum displacement of the plate and L is the beam length.

The resonant frequency of the sensor is analytically calculated using Rayleigh's method based on the third  $mode^{[8]}$ :

$$KE_{max} = PE_{max}$$
(4)



Fig. 3 Third mode shape of a folded-beam when the resonant plate is displaced by  $x_0$ 

where  $KE_{max}$  is the maximum kinetic energy during a vibration cycle and  $PE_{max}$  is the maximum potential energy.

$$\mathbf{K}\mathbf{E}_{\max} = \mathbf{K}\mathbf{E}_{\text{plate}} + \mathbf{K}\mathbf{E}_{\text{truss}} + \mathbf{K}\mathbf{E}_{\text{beam}}$$
$$= -\frac{1}{2}v_{p}^{2}M_{p} + \frac{1}{2}v_{t}^{2}M_{t} + \frac{1}{2}\int v_{b}^{2}\mathbf{d}M_{b}$$
(5)

where  $M_{\rm p}$  is the plate mass,  $M_{\rm t}$  is the mass of the folding trusses, and  $M_{\rm b}$  is the total mass of the suspension beams.

$$KE_{max} = \frac{1}{2} x_0^2 \omega^2 M_p + \frac{1}{8} x_0^2 \omega^2 M_t + \frac{\omega^2}{2} \int x(y) dM_b$$
  
=  $x_0^2 \omega^2 \left( \frac{1}{2} M_p + \frac{1}{8} M_t + \frac{6}{35} M_b \right)$  (6)

$$PE_{max} = \int_{0}^{x_{0}} F_{x} dx = \int_{0}^{x_{0}} k_{x} x dx = \frac{1}{2} k_{x} x_{0}^{2}$$
(7)

And  $k_x$  is given by Ref. [6].

$$k_x = Eh\left(\frac{W}{L}\right)^3 \tag{8}$$

where W and h are the cross-sectional width and thickness, respectively. Then the expression for the resonance frequency  $(f_r)$  becomes:

$$f_{\rm r} = \frac{1}{2\pi} \left[ \frac{2Eh(W/L)^3}{\left(M_{\rm P} + \frac{1}{4}M_{\rm t} + \frac{12}{35}M_{\rm b}\right)} \right]^{1/2}$$
(9)

From Eq. (9), the  $f_r$  can be improved through adjusting the beam width, beam length, plate area, and selecting a high Young's modulus material to process.

#### 2.3 Finite-element analysis

Finite-element analysis is performed using Intellisuite software, available commercially from IntelliSense Incorporated. The Intellifab module of the Intellisuite software is introduced to build the resonant structure through simulating the processes of the resonator device. The device performance is analyzed using the ThermoElectroMechanical module. Details of the overall design are summarized in Table 1.

The Young's modulus of poly 3C-SiC can be obtained from Eq. (9), the geometry, and the measured resonant frequency.

Parameter	Value	Unit
Folded-beam length, L	100	$\mu$ m
Folded-beam width, W	2/3.5/5.5	$\mu$ m
Structural layer thickness, h	3	$\mu$ m
No. finger overlaps	20	
Finger gap space, d	2	$\mu$ m
Finger overlap length, $L_d$	20	$\mu$ m
Young's modulus, $E$	430(calculated)	GPa
Density of poly 3C-SiC, $\rho$	3.2	g/cm <sup>3</sup>

Table 1 Parameters of the resonator

Figure 4 shows the dependence of simulated resonant frequencies versus the Young's modulus and the beam length. The simulated resonant frequency increases rapidly as the Young's modulus is enhanced (as seen in Fig. 4(a)). Poly 3C-SiC with high Young's modulus are more profitable to fabricate the high frequency resonator. An inverse relationship between frequency and beam length was obtained, as seen in Fig. 4(b).

The simulated frequency does not change with the beam thickness. However, when the W/h ratio exceeds 2, the resonator can not vibrate in the lateral direction. Thus, adjusting the resonant frequency by increasing the beam width is also affected by the beam thickness.

### **3** Fabrication and measurement

The resonators with three different beam widths



Fig. 4 Dependence of simulated resonant frequency versus the Young's modulus (a) and the beam length (b)







Fig. 5 SEM of the fabricated poly 3C-SiC resonator structure(a) Full view; (b) Enlarged view of the folded-beam structure;(c) Enlarged view of the linear comb structure and the plate

were fabricated using  $3\mu$ m thick poly 3C-SiC thin film grown on PECVD SiO<sub>2</sub> / Si<sub>3</sub>N<sub>4</sub>/SiO<sub>2</sub>/Si substrates in a hot-wall, RF-induction heated LPCVD reactor. The experimental setup was described in Ref. [9]. SiO<sub>2</sub> was used as isolation and sacrificial layers separately in the device structure. A Si<sub>3</sub>N<sub>4</sub> layer was grown between the two SiO<sub>2</sub> layers to enhance the isolation effect and to protect the SiO<sub>2</sub> layer under it. The thermal evaporated Ni film was deposited on poly 3C-SiC to form an Ohmic contact by annealing at 1000°C in a vacuum environment. Cr/Au were deposited as pad metals<sup>[9]</sup>.

The resonator structure is shown in Fig. 5. The beam widths are 2, 3. 5, and 5.  $5\mu$ m, respectively. The other parameters are the same as in Table 1. Dynamic behaviors of the devices were measured by a MEMS micro-motion analyzer system.

Figure 6 shows the dependence of the simulated and measured resonant frequencies on the beam width. The resonant frequency increases as the beam width increases. The measured resonant frequencies of



Fig. 6 Dependence of the simulated and measured resonant frequencies on the beam width

the 2, 3. 5, and 5.  $5\mu$ m in beam width resonators are 64. 5, 147. 4, and 255. 5kHz, respectively, which are in good agreement with the simulated resonant frequencies.

# 4 Conclusion

A numerical solution based on the Rayleigh's method was used to determine the resonance frequencies. The resonance frequencies for the resonators are governed mainly by their material properties such as the Young's modulus and resonator geometry parameters such as beam width, length, thickness, and the area of the plate. Resonators with three difference beam widths were fabricated. Their resonant frequencies were measured to be 64. 5, 147. 2, and 255. 5kHz, respectively, which is in good agreement with the simulated resonant frequencies. It was shown that an improved frequency performance could be obtained on

the poly 3C-SiC thin films with high Young's modulus.

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# 水平静电驱动式多晶 3C-SiC 折叠悬臂梁谐振器微结构\*

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摘要:介绍了一种微机械叉指静电驱动折叠悬臂梁谐振器的设计和制作方法.将 Rayleigh 分析法和有限元分析法结合起来分析调整器件尺寸和材料参数对器件性能的影响.制作了三种不同悬臂梁宽度的微机械横向谐振器件,经实验检测它们的谐振频率分别为 64.5,147.2,255.5kHz,与模拟结果符合得很好.该结果显示由于具有很高的杨式模量,利用多晶 3C-SiC 材料体系制作的谐振器件能够具有更高的谐振频率.

关键词:横向谐振器件;折叠悬臂梁;叉指结构;微机械系统;谐振器;碳化硅
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