

# A 10bit 100MS/s Pipelined ADC with an Improved 1.5bit/Stage Architecture\*

Ye Fan, Shi Yufeng, Guo Yao, Luo Lei, Xu Jun, and Ren Junyan<sup>†</sup>

(State Key Laboratory of ASIC & System, Fudan University, Microelectronics Science and Technology Innovation Platform, Shanghai 201203, China)

**Abstract:** This paper presents a 10bit 100MS/s CMOS pipelined analog-to-digital converter (ADC) based on an improved 1.5bit/stage architecture. The ADC achieves a peak signal-to-noise-and-distortion ratio (SNDR) of 57dB and maintains 51dB up to 57MHz, the Nyquist frequency for a clock rate of 100Msample/s. The differential non-linearity (DNL) and integral non-linearity (INL) are typically measured as 0.3LSB and 1.0LSB, respectively. The ADC is implemented in a 0.18 $\mu$ m mixed-signal CMOS technology and occupies 0.76mm<sup>2</sup>.

**Key words:** analog-to-digital converter; pipeline; improved 1.5bit/stage architecture

**EEACC:** 1265H; 1280; 2570D

**CLC number:** TN432

**Document code:** A

**Article ID:** 0253-4177(2008)12-2359-05

## 1 Introduction

High performance ADCs are necessary in versatile applications such as wireless communication systems, high speed instrumentations and high quality video systems. Higher resolution, higher sampling rate and lower power consumption are usually the main concerns for the ADCs used in these applications. The pipelined ADC has been largely studied and widely used because of the good trade-off among the speed, resolution, power consumption and chip area. In previous studies, most design interests were focused on the first pipelined stage, wideband SHA or other techniques for performance improvement<sup>[1~3]</sup>, but seldom on the last stage of pipelined ADC. However, the non-monotonicity of pipelined ADC caused by the last stage will reduce the linearity and should not be ignored.

In this paper, the non-monotonicity of the traditional 1.5bit/stage pipelined ADC is analyzed, and an improved 1.5bit/stage pipelined architecture with a new last stage is proposed. To demonstrate the improvement, a 10bit 100MS/s pipelined ADC with an extra correction stage is implemented in a 0.18 $\mu$ m mixed-signal CMOS technology.

## 2 Analysis of non-monotonicity

Usually, 1.5bit/stage architecture<sup>[4]</sup> is applied to most 10bit pipelined ADCs because of its power-

optimized per stage resolution, which also relaxes the requirement of sub-ADC comparators. If the output of an ADC is  $k$  bit, the conventional ADC is composed of  $k - 2$  pipelined stages and a 2bit flash ADC as the last stage.

According to the 1.5bit/stage algorithm and pipeline theory, we can derive the residue output of the  $(k - 2)$ <sub>th</sub> stage which is also the analog input of the last stage from the digital outputs of the previous stages.

$$V_i(k - 1) = V_o(k - 2) = 2^{k-2} V_{in} - [2^{k-3} D_1 + \dots + D_{k-2} - (2^{k-3} + \dots + 1)] V_r \quad (1)$$

where  $V_{in}$  is the input signal,  $D_k$  is the digital output of the  $(k)$ <sub>th</sub> stage, and  $V_r$  is the reference voltage.

As to the last stage, it is a standard 2bit flash ADC which has three decision levels;  $-V_r/2$ ,  $0$  and  $V_r/2$ . Assuming that the offset errors of these decision levels are  $\epsilon_1$ ,  $\epsilon_2$  and  $\epsilon_3$ , the decision ranges of the last stage are given by

$$\begin{cases} D_{k-1} = 0(00)_2 \Rightarrow V_i(k - 1) \in [-V_r, -V_r/2 + \epsilon_1] \\ D_{k-1} = 1(01)_2 \Rightarrow V_i(k - 1) \in [-V_r/2 + \epsilon_1, \epsilon_2] \\ D_{k-1} = 2(10)_2 \Rightarrow V_i(k - 1) \in [\epsilon_2, +V_r/2 + \epsilon_3] \\ D_{k-1} = 3(11)_2 \Rightarrow V_i(k - 1) \in [+V_r/2 + \epsilon_3, V_r] \end{cases} \quad (2)$$

where  $D_{k-1}$  and  $V_i(k - 1)$  is the digital output and analog input of the last stage.

Also according to the digital correction algorithm, the output code of the pipelined ADC can be written as

$$D = 2^{k-2} D_1 + 2^{k-3} D_2 + \dots + 2D_{k-2} + D_{k-1} \quad (3)$$

So if the output code of ADC is an even number

\* Project supported by the Research and Development Fund for the Applied Materials of Shanghai City (No.07SA16)

<sup>†</sup> Corresponding author. Email: jyren@fudan.edu.cn

Received 16 June 2008, revised manuscript received 14 August 2008

(assuming  $D = 2N$ ), the last stage output  $D_{k-1}$  must be an even number. Contrary wise, If  $D$  is an odd number ( $D = 2N + 1$ ),  $D_{k-1}$  must be an odd number.

$$\left\{ \begin{aligned} D = 2N, D_{k-1} = 0(00)_2 &\Rightarrow V_{in} \in \left[ \frac{2N}{2^k} \times 2V_r - V_r, \frac{2N+1}{2^k} \times 2V_r - V_r + \frac{\epsilon_1}{2^{k-2}} \right] \\ D = 2N+1, D_{k-1} = 1(01)_2 &\Rightarrow V_{in} \in \left[ \frac{2N+1}{2^k} \times 2V_r - V_r + \frac{\epsilon_1}{2^{k-2}}, \frac{2N+2}{2^k} \times 2V_r - V_r + \frac{\epsilon_2}{2^{k-2}} \right] \\ D = 2N, D_{k-1} = 2(10)_2 &\Rightarrow V_{in} \in \left[ \frac{2N}{2^k} \times 2V_r - V_r + \frac{\epsilon_2}{2^{k-2}}, \frac{2N+1}{2^k} \times 2V_r - V_r + \frac{\epsilon_3}{2^{k-2}} \right] \\ D = 2N+1, D_{k-1} = 3(11)_2 &\Rightarrow V_{in} \in \left[ \frac{2N+1}{2^k} \times 2V_r - V_r + \frac{\epsilon_3}{2^{k-2}}, \frac{2N+2}{2^k} \times 2V_r - V_r \right] \end{aligned} \right. \quad (4)$$

It is also can be shown by Fig. 1, where

$$\begin{aligned} X_1 &= \frac{2N}{2^k} \times 2V_r - V_r; X_2 = \frac{2N+1}{2^k} \times 2V_r - V_r; \\ X_3 &= \frac{2N+2}{2^k} \times 2V_r - V_r \end{aligned}$$

If  $\epsilon_1 > \epsilon_3$ , the decision range of  $D = 2N$  and  $D_{k-1} = 00$ , which is noted as  $2N(00)$  for short, would overlap with the decision range of  $2N+1(11)$ . If the input of ADC increases through the overlapping range in Fig. 1, for example, a  $D_{k-1}$  path is  $(10 \rightarrow 11 \rightarrow 00)$ , the output path of ADC would be  $(2N \rightarrow 2N+1 \rightarrow 2N)$ . In the last stage, the offset errors of the three comparators in 2bit flash ADC are independent and uncontrollable. As a result, decision range overlapping is inevitable and will cause non-monotonicity in the conventional 1.5bit/stage architecture.

### 3 Converter architecture

To avoid this non-monotonicity, improved last stage architecture of the pipelined ADC is proposed in Fig. 2. The flash ADC is substituted by a typical pipelined stage to output 2bit and an extra comparator which is used to introduce a redundant bit. Because the decision levels are only determined by the threshold of the extra comparator, the non-monotonicity of the ADC could be entirely eliminated by a digital-correction when the offsets of comparators are less than  $1/4V_r$ . Assuming that the decision level of the last comparator is  $\delta_c$ , then we can rewrite Eqs. (1), (2) and (3):

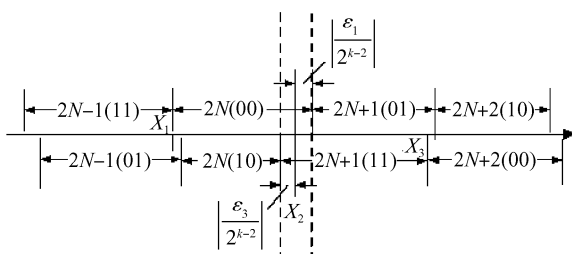


Fig.1 Decision levels and output code

Combining Eqs. (1) ~ (3), one can derive the input decision ranges from the output code of the whole ADC and the last stage,

$$V_i(k) = V_o(k-1) = 2^{k-1} V_{in} - [2^{k-2} D_1 + \dots + D_{k-1} - (2^{k-2} + \dots + 1)] V_r \quad (5)$$

$$\begin{cases} D_k = 0 \Rightarrow V_i(k) < \delta_c \\ D_k = 1 \Rightarrow V_i(k) \geq \delta_c \end{cases} \quad (6)$$

$$D = 2^{k-1} D_1 + 2^{k-3} D_2 + \dots + 2D_{k-2} + D_{k-1} + D_k \quad (7)$$

If the output code of whole ADC is  $N$ . we can get from the above three equations:

$$\begin{cases} D = N, D_k = 0 \Rightarrow V_{in} < \frac{N+1}{2^k} \times 2V_r - V_r + \frac{\delta_c}{2^{k-1}} \\ D = N, D_k = 1 \Rightarrow V_{in} \geq \frac{N}{2^k} \times 2V_r - V_r + V_r + \frac{\delta_c}{2^{k-1}} \end{cases} \quad (8)$$

It can be seen that there is no overlapping area in the decision range, the digital output increases one by one when the ADC input signal increases, so the non-monotonicity of ADC is entirely eliminated. Figure 2 compares the simulation results of the conventional architecture and the improved architecture and shows an up-to-5dB improvement of SNR achieved by eliminating the non-monotonicity of the pipelined ADC.

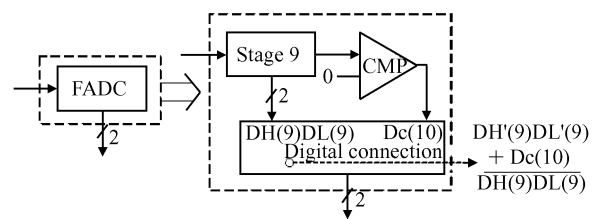


Fig.2 Proposed architecture and simulation results

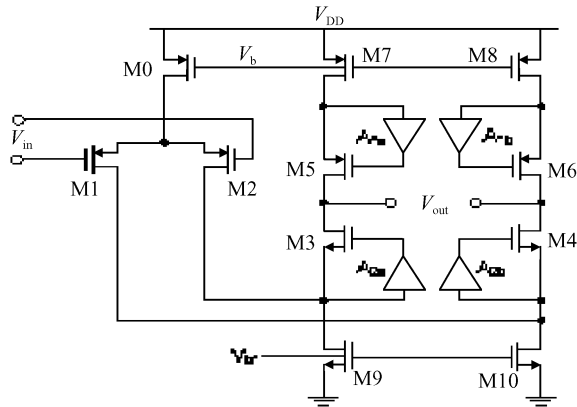


Fig. 3 Gain boosting folded cascode opamp

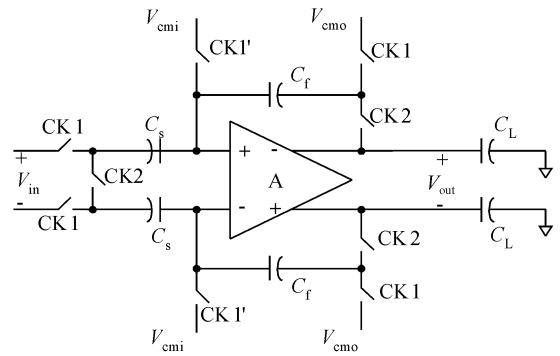
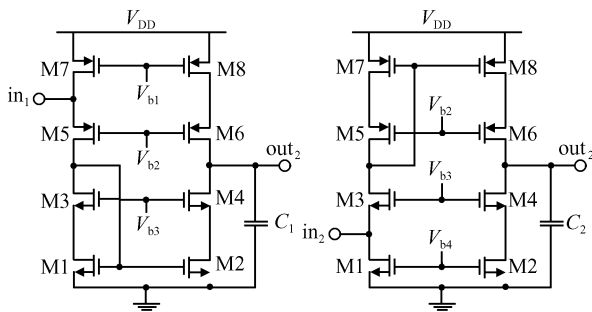


Fig. 4 Sample and hold architecture

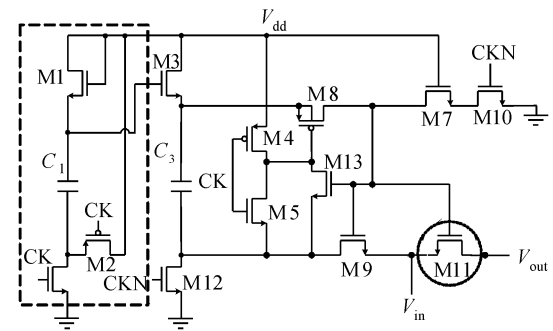


Fig. 5 Bootstrapped input sampling switch

## 4 Circuit implementation

### 4.1 Opamp

Single-stage folded cascode OPAMP is used in SHA and other pipelined stages to obtain excellent bandwidth and output swing for low voltage application. As shown in Fig. 3, two gain-boosting feedback amplifiers are used to increase the output impedance of the folded cascode amplifier. In order to minimize the output swing reduction caused by the additional amplifiers, the input voltages of the two regulation current amplifiers are adopted to equalize  $V_{DD} - V_{dsat-p}$  or  $V_{dsat-n}$ . The compensation capacitors  $C_1$  and  $C_2$  at the output of the two additional amplifiers eliminate the extra zeros introduced by the additional amplifiers. The simulation results show that the OPAMP has a DC gain of 95dB and unity gain bandwidth of about 860MHz with a 2pF capacitance load.

### 4.2 SHA and bootstrapped switch

Sample and hold (SHA) circuit is shown in Fig. 4. The input and output common mode voltages can be adjusted by the values of  $V_{cmi}$  and  $V_{cmo}$ , respectively, for different input common mode levels. In order to deal with high input swing and reduce signal distortion, the gate-source voltage of the input switches has to be boosted to a fixed voltage independent of input signal. A bootstrapped, high swing MOS

switch<sup>[5]</sup> is employed in this SHA, which is shown in Fig. 5. When CK is high, the voltage of  $C_1$  is pre-charged to  $V_{DD} - V_t$ , where  $V_t$  is the source-gate voltage of M1. In the next phase, the bottom plate of  $C_1$  connects to  $V_{DD}$  and the top plate of  $C_1$  pre-charged to  $2V_{DD} - V_t$ , which turns M3 on and charges  $C_3$  to  $V_{DD}$ . When M3 is off, the voltage of  $C_3$  keeps the gate-source voltage of the switch M11 to a fixed voltage. Only one capacitor is used in this boosting circuit (dotted box), which results in a smaller area than a clock multiplier in the conventional design.

## 5 Prototype measurements

The prototype ADC was fabricated in a 0.18 $\mu$ m CMOS process. Capacitors were implemented using metal-insulator-metal (MIM) structures. The die photo is shown in Fig. 6. The ADC occupies an active die

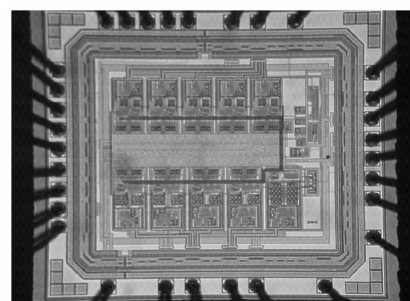


Fig. 6 Die photograph

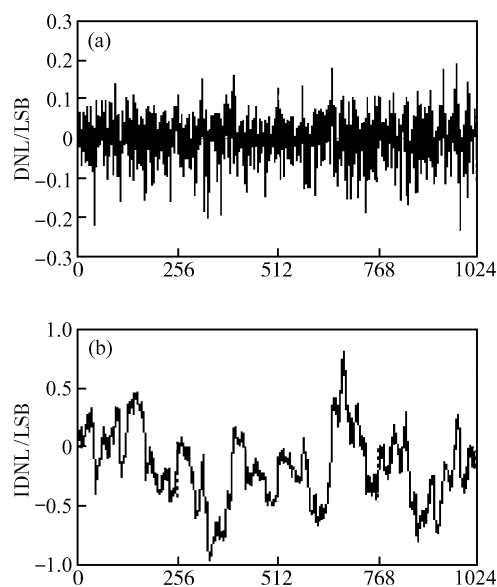


Fig. 7 Measured DNL and INL

area of  $0.76\text{mm}^2$  and dissipates a power of  $126\text{mW}$  at a supply voltage of  $1.8\text{V}$  and a sampling rate of  $100\text{MS/s}$ .

The measured DNL and INL profiles are shown in Fig. 7. The maximum DNL is  $0.3\text{LSB}$  and the maximum INL is  $1.05\text{LSB}$ . The dynamic performance of the ADC was characterized by analyzing a fast Fourier transform (FFT) of the output code input. The measured signal-to-noise-and-distortion (SNDR) is about  $57.4\text{dB}$  with a  $5\text{MHz}$  input, equivalent to  $9.23$  effective numbers of bits (ENOB). Under the same condition, the signal-to-noise (SNR) is about  $58.6\text{dB}$ , the spurious free dynamic range (SFDR) is about  $68.5\text{dB}$ , the total of harmonic distortion (THD) is  $-63.3\text{dB}$ . The measured dynamic performance versus input frequency is shown in Fig. 8. The measured performance of the prototype ADC is summarized in Table 1.

## 6 Conclusion

A  $10\text{bit}$   $100\text{MS/s}$  pipelined ADC is designed and fabricated in a  $0.18\mu\text{m}$  mixed signal CMOS technology. An improved  $1.5\text{bit}/\text{stage}$  pipelined architecture has been used in this work to eliminate non-monotonicity of the traditional pipelined ADC architecture.

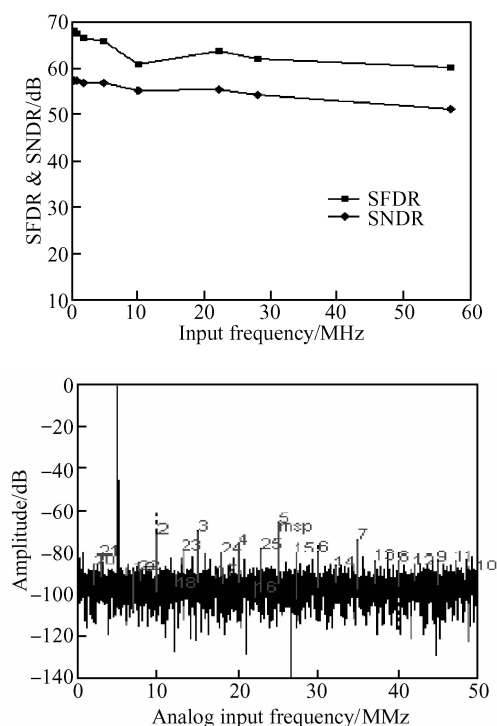


Fig. 8 SNDR/SFDR versus input frequency

Table 1 Summary of ADC performance

|                 |   |
|-----------------|---|
| Resolution      | 10bit   |
| Conversion rate | 100MHz  |
| Technology      | $0.18\mu\text{m}$ CMOS  |
| Power supply    | $1.8\text{V}$   |
| Total power     | $126\text{mW}$  |
| DNL/INL         | $0.3\text{LSB}/1.05\text{LSB}$  |
| SNR/SNDR/SFDR   | $58.6\text{dB}/57.4\text{dB}/68.5\text{dB}$ ( $f_{in} = 5\text{MHz}$ )<br>$54.3\text{dB}/52.4\text{dB}/59.8\text{dB}$ ( $f_{in} = 57\text{MHz}$ ) |
| THD             | $-63.3\text{dB}$ ( $f_{in} = 5\text{MHz}$ )   |
| ENOB            | $9.23$ ( $f_{in} = 5\text{MHz}$ )   |
| Area            | $0.74\text{mm}^2$   |

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## 采用改进型 1.5 位/级结构的 10 位 100MHz 流水线模数转换器\*

叶 凡 施宇峰 过 瑶 罗 磊 许 俊 任俊彦<sup>†</sup>

(复旦大学专用集成电路与系统国家重点实验室, 微纳电子科技创新平台, 上海 201203)

**摘要:** 介绍了一个采用改进型 1.5 位/级结构的 10 位 100MHz 流水线结构模数转换器. 测试结果表明, 模数转换器的信噪失真比最高可以达到 57dB, 在 100MHz 输入时钟下, 输入信号为 57MHz 的奈奎斯特频率时, 信噪失真比仍然可以达到 51dB. 模数转换器的差分非线性和积分非线性分别为 0.3LSB 和 1.0LSB. 电路采用 0.18 $\mu$ m 混合信号 CMOS 工艺实现, 芯片面积为 0.76mm<sup>2</sup>.

**关键词:** 模数转换器; 流水线结构; 改进型 1.5 位/级结构

**EEACC:** 1265H; 1280; 2570D

**中图分类号:** TN432      **文献标识码:** A      **文章编号:** 0253-4177(2008)12-2359-05

\* 上海市应用材料研究与发展基金资助项目(批准号:07SA16)

<sup>†</sup> 通信作者. Email: jyren@fudan.edu.cn

2008-06-16 收到, 2008-08-14 定稿