# Tunable current mirror and its application in LNA\*

Li Kun(李琨)<sup>1,†</sup>, Teng Jianfu(滕建辅)<sup>1,2</sup>, Yu Changliang(余长亮)<sup>1</sup>, and Huang Jianyao(黄建尧)<sup>1</sup>

(1 School of Electronic and Information Engineering, Tianjin University, Tianjin 300072, China)

(2 School of Electronic and Information Engineering, Tianjin University of Technology, Tianjin 300384, China)

**Abstract:** A novel topology of current mirror (CM) with tunable output current is proposed. Two methods for output current tuning are presented. The first one utilizes an analog input voltage for linear current output, and the second one has an *N*-bit digital input signal for  $2^N$  un-continuous current outputs. A linearization method for low noise amplifier (LNA) is proposed and realized with this tunable CM. As the provider of the bias current, the CM has brought the LNA a lower NF (noise figure) and a higher IIP3 (input-referred third-order intercept point) compared with a conventional one. The experimental results show that the LNA achieves 1.47 dB NF and +19.83 dBm IIP3 at 860 MHz.

**Key words:** current mirror; tunable; LNA; bias current; linearization **DOI:** 10.1088/1674-4926/30/12/125012 **EEACC:** 1130; 1350D

# 1. Introduction

Recently, the realization of analog signal processing based on current-mode circuit has received considerable attention. Current mirrors (CMs) based on BJT or MOSFET devices are important building blocks for current-mode circuit design.

The tunable CMs are required widely in applications such as current-mode amplifying<sup>[1]</sup> and filtering<sup>[2]</sup>. Also, some related techniques have been reported in the past few years. For example, Somdunyakanok proposed an accurate tunable CM based on translinear type-A in 2008<sup>[3]</sup>. Another accurate wide swing CM using the npn-NMOS cascade instead of the NMOS–NMOS cascade was presented by Yang in 2008<sup>[4]</sup>. A programmable CM composed of DGMOSFET has been introduced by Hamed in 2007<sup>[1]</sup>. Guvenc has proposed a tunable linear CM composed with both BJT and MOSFET in 2008<sup>[5]</sup>. It can be seen that accurate current output has been accomplished but complexity was suffered.

In this paper, a novel tunable CM composed of 3 BJTs is proposed and implemented. It has the advantages of simplicity, wide tuning range and convenience in use. The accuracy of this CM is high enough for most applications, such as biasing, amplifying, and so on. The output of this CM can be controlled either by an analog voltage or an *N*-bit digital signal (N+2 BJTs needed). It is thought that the proposed structure would be applied in a wide variety of areas.

This tunable CM has been adopted as the provider of bias current in an LNA design for a lower NF (noise figure) and a higher IIP3 (input-referred third-order intercept point). Therefore, the LNA achieves a larger dynamic range with the method of tuning bias current according to the strength of the received signal. Experiments were carried out for both CM and LNA. Simulation and measurement results are both very consistent with the theoretical analysis.

# 2. Conventional current mirror

A conventional classic schematic of CM is shown in Fig. 1.

In order to simplify the analysis of CM, the Early effect of BJT is ignored, which will bring little error into the analysis result. According to Kirchhoff's law and the theories of BJT,  $I_{OUT}$  can be calculated as:

$$I_{\rm OUT} = \frac{V_{\rm CC} - V_{\rm BE1}}{(R_1 + R_{\rm REF}) \left(1 + \frac{1}{\beta}\right) \frac{R_2}{R_1} + \frac{R_{\rm REF}}{\beta}},$$
(1)

where  $\beta$  is the ratio of collector current to base current.

In the engineering, by setting the value of  $V_{\text{BE1}}$  to 0.6 V and assuming  $\beta$  infinite, Equation (1) can be simplified into:

$$I_{\rm OUT} = \frac{R_1}{R_2} \frac{V_{\rm CC} - V_{\rm BE1}}{R_1 + R_{\rm REF}} = \frac{R_1}{R_2} \frac{V_{\rm CC} - 0.6}{R_1 + R_{\rm REF}}.$$
 (2)



Fig. 1. Schematic of a conventional CM.

© 2009 Chinese Institute of Electronics

Project supported by the Tianjin Natural Science Foundation, China (No. 09JCYBJC00700).

<sup>†</sup> Corresponding author. Email: nathanme@163.com

Received 24 August 2009, revised manuscript received 18 September 2009



Fig. 2. Schematic of a tunable cm with output current controlled by an analog voltage.

# 3. Tunable current mirror

For an adjustable output current, we make  $R_{\text{REF}}$  (in Fig. 1) a variable resistor. It is obvious that  $I_{\text{OUT}}$  will change when  $R_{\text{REF}}$  is tuned.

To avoid overheating the transistors in the tunable CM, a resistor ( $R_{OUT}$ ) is adopted to limit the maximum of  $I_{OUT}$ .

In the following sections, two methods for tuning the output current are introduced and realized, where one utilizes an analog voltage, and the other adopts an *N*-bit digital signal.

# 3.1. CM with output current controlled by an analog voltage

Figure 2 gives the schematic of a tunable CM with an analog input voltage ( $V_{\text{TUNE}}$ ) for output current controlling. Q3 is a transistor acting as a variable resistor controlled by  $V_{\text{TUNE}}$ . When  $V_{\text{TUNE}}$  grows high, the resistor between the collector and emitter of Q3 will decrease, then  $I_{\text{REF}}$  and  $I_{\text{OUT}}$  will both increase.

It can be proved that  $I_{OUT}$  is almost a linear function of  $V_{TUNE}$  when Q3 works in the linear region. According to Kirchhoff's voltage law, Equation (3) is easy to get by analyzing the base circuit of Q3.

$$V_{\rm TUNE} - V_{\rm BE3} - I_{\rm B3}R_{\rm B} - I_{\rm E3}R_{\rm REF} = 0.$$
(3)

Based on the theory of BJT, when Q3 works within the linear region,  $I_{B3}$  can be derived as:

$$I_{\rm B3} = \frac{I_{\rm REF}}{\beta} = \frac{R_2 I_{\rm OUT}}{R_1 \beta}.$$
 (4)

Then,  $I_{OUT}$  can be deduced from Eqs. (3) and (4) as:

$$I_{\rm OUT} = (V_{\rm TUNE} - V_{\rm th}) \frac{R_1 \beta}{R_2 [R_{\rm B} + (\beta + 1) R_{\rm REF}]},$$
 (5)

where  $V_{\text{th}}$  is the threshold voltage of a transistor.

According to Eq. (5), it can be concluded that  $I_{OUT}$  and  $V_{TUNE}$  have a linear relationship when Q3 is in linear region.

Furthermore, Q3 can be replaced by a PNP transistor for a negative ratio of  $I_{OUT}$  and  $V_{TUNE}$ .



Fig. 3. Schematic of a tunable CM with output current controlled by *N*-bit digital signal.

# **3.2.** CM with output current controlled by *N*-bit digital sig nal

Figure 3 shows the schematic of a tunable CM with an *N*-bit digital input signal. In Fig. 3, every controlling signal  $(V_{\text{CTRL-}i})$  is added to the base of BJT (QB*i*) in each branch. And a resistor  $R_{\text{REF-}i}$  which determines the weight of each branch is adopted in series with QB*i*.

It is seen that QB-*i* will operate in the saturation region when  $V_{\text{CTRL}-i}$  is high (bit<sub>i</sub> = 1), and in the cut off region when  $V_{\text{CTRL}-i}$  is low (bit<sub>i</sub> = 0). Assuming that the equivalent resistor between the collector and emitter of QB-*i* ( $R_{\text{CE}-i}$ ) is much smaller than  $R_{\text{REF}-i}$  when QB-*i* is in the saturation region, and that  $R_{\text{CE}-i}$  is much greater than  $R_{\text{REF}-i}$  when QB-*i* is in the cut off region. Then the equivalent resistor of each branch ( $R_{\text{SUB}-i}$ ) can be expressed as:

$$R_{\text{SUB-}i} = \begin{cases} R_{\text{REF-}i} & \text{bit}_i = 1, \\ \infty, & \text{bit}_i = 0. \end{cases}$$
(6)

Based on Eq. (2),  $I_{OUT}$  can be calculated as:

$$I_{\rm OUT} = \frac{R_1}{R_2} \frac{V_{\rm CC} - V_{\rm BE1}}{R_1 + R_{\rm SUB-1} / / R_{\rm SUB-2} / / \cdots / / R_{\rm SUB-N}}.$$
 (7)

If the value of  $R_1$  is designed much smaller than  $R_{\text{REF-1}}//R_{\text{REF-2}}//\cdots//R_{\text{REF-N}}$ , then Equation (7) can be simplified into:

$$I_{\rm OUT} = \frac{R_1}{R_2} (V_{\rm CC} - V_{\rm BE1}) \left( \frac{\text{bit}_1}{R_{\rm REF-1}} + \frac{\text{bit}_2}{R_{\rm REF-2}} + \dots + \frac{\text{bit}_N}{R_{\rm REF-N}} \right).$$
(8)

And Equation (8) can also be expressed in vector format

$$I_{\text{OUT}} = \frac{R_1}{R_2} (V_{\text{CC}} - V_{\text{BE1}}) [\text{bit}_1 \ \text{bit}_2 \ \cdots \ \text{bit}_N] \\ \times \left[ \frac{1}{R_{\text{REF-1}}} \ \frac{1}{R_{\text{REF-2}}} \ \cdots \ \frac{1}{R_{\text{REF-N}}} \right]^T.$$
(9)

In addition, the values of  $R_{\text{REF}-i}$  can be designed and put into a particular array, correspondingly, the different values of  $I_{\text{OUT}}$  will be organized in a special series. For example, we can get  $I_{\text{OUT}}$  in arithmetic progression if  $R_{\text{REF}-i}$  satisfies  $R_{\text{REF}-(i-1)} = 2R_{\text{REF}-i}$ .

Furthermore, QB-i can be a PNP BJT or a MOSFET.

as:

1E8

1E7



Fig. 4. Curves of  $I_{OUT}$  versus  $V_{TUNE}$  in the tunable CM.



300

200

100 200

-200

1E4

1E5

Fig. 5. AC performance of the tunable CM.

1E6

Frequency (Hz)

Magnitude of  $I_{our}(\mu A)$ 

Phase of  $I_{\rm OUT}$  (degree)

Fig. 6. Output current of the CM control by 2-bit digital signal: (a) Simulation result; (b) Measurement result: the photo of waveform on oscilloscope screen.  $V_{OUT}$ : Voltage over  $R_{OUT}$ , Representing  $I_{OUT}$ . ( $R_{OUT} = 100 \Omega$ ).

#### 3.3. Simulation and experiment results of the tunable CM

# 3.3.1. Tunable CM controlled by an analog voltage

To verify the theoretical analysis results above, the schematic in part 3.1 (Fig. 2) was simulated first, and then experiments were carried out on a PCB board.

Firstly, the DC characteristic was simulated and tested. The results are given in Fig. 4.

We observed that the curve of  $I_{OUT}$  versus  $V_{TUNE}$  could be divided into 3 sections (sections A, B and C). In section A, Q3 is cut off, and  $R_{CE3}$  is so large that  $I_{OUT}$  is limited in a very low value. In section B, Q3 is operating within the linear region.  $I_{OUT}$  increases as a linear function of  $V_{TUNE}$  which verifies the conclusion in part 3.1. In section C,  $I_{OUT}$  is limited by the resistor in the OUTPUT branch.

Secondly, AC simulation was carried out. The simulation result is shown in Fig. 5. The frequency range of linear operation of this CM is up to 1 MHz which is sufficient for application in bias current. And the top boundary of the operation frequency can be reduced by increasing the resistance of  $R_{\rm B}$  or  $R_{\rm OUT}$ .

#### 3.3.2. Tunable CM controlled by N-bit digital signal

Simulation and experiment were both performed for the tunable CM with a 2-bit digital control signal, where  $R_{\text{REF}-i}$  was designed as  $R_{\text{REF}-1} = 2R_{\text{REF}-2}$ . Figure 6(a) gives the simulation results, including the waveform of the control voltage

 $(V_{\text{CTRL-1}}, V_{\text{CTRL-2}})$  and output current  $(I_{\text{OUT}})$ . Figure 6(b) gives measurement results where  $V_{\text{OUT}}$  (the voltage of  $R_{\text{OUT}}$ ) can represent  $I_{\text{OUT}}$  by dividing  $R_{\text{OUT}}$  (100  $\Omega$ ).

# 4. Application of tunable CM in LNA

LNA, which is located in the front of a receiver, has a great influence on the receiver's performance. Nowadays, although more and more LNA is integrated in CMOS technology, the discrete low noise BJT is still in use for extremely low noise, high linearity and high frequency.

Given the IIP3 and NF, one can define another important property of LNA called the spurious-free dynamic range (SFDR). The SFDR is commonly used to determine the input power range in which the received signal can be detected in the presence of noise and amplified without nonlinear interference<sup>[6, 7]</sup>. The value of SFDR can be obtained from IIP3 and NF through:

SFDR(dB) = 
$$\frac{2}{3}$$
[IIP3(dBm) - NF(dB) - 10 lg *B*(Hz) + 174],  
(10)

where B is the channel bandwidth.

According to Eq. (10), a large SFDR can be achieved by low NF and high IIP3. But it is known that low NF and high IIP3 are hard to achieve simultaneously. We noticed that bias current had a big influence on the parameters of BJT, including NF and IIP3. Lowest NF (NF<sub>OPT</sub>) could be obtained as colle-



Fig. 7. Expanding SFDR with low and high bias current. G: Power gain of LNA.



Fig. 8. (a) Schematic of an LNA with tunable CM circuit; (b) PCB of the RF front-end of the receiver.

ctor current density is around 38  $\mu$ A/unit\_area<sup>[8]</sup>. And according to BJT's Volterra model<sup>[9]</sup>, IIP3 increases as collector current grows.

Then we proposed a method, adjusting the LNA's bias current according to the strength of received signal, to harmonize the contradiction between low NF and high IIP3 in the narrow bandwidth wireless system. In detail, when receiving weak signal, the receiver can adjust the bias current to obtain NF<sub>OPT</sub> for high sensitivity. On the other hand, high IIP3 is achieved by increasing bias current for dealing with strong received signal. Figure 7 shows the SFDR of LNA with low and high bias currents. The parameters' names ending up with '-L' and '-H' represent low and high bias current, respectively. The expanded SFDR (SFDR-TOTAL) is the union of SFDR-L and SFDR-H. Therefore, the SFDR is expanded with the tunable bias current.

The complete schematic of the designed LNA is shown in Fig. 8(a). This LNA has been successfully applied in a narrowband wireless receiver. Figure 8 (b) shows the photo of the RF



Fig. 9. Measurement and simulation results of  $\mu$  criterion.



Fig. 10. Waveform of  $I_{\text{OUT}}$  as  $V_{\text{CTRL}}$  changes: (a) Simulation result; (b) Measurement result: the photo of waveform on oscilloscope screen.  $V_{\text{OUT}}$ : Voltage over  $R_{\text{OUT}}$ , Representing  $I_{\text{OUT}}$ . ( $R_{\text{OUT}} = 100 \Omega$ ).

front-end PCB of the receiver. The frequency band of receiving signal is at 860 MHz. And the requirements of the LNA are: Gain > 8 dB, IIP3 > 18 dBm, NF < 1.5 dB.

As the provider of bias current, a simple and convenient CM is preferred rather than an accurate one. Here, the digital control method introduced in part 3.2 was adopted. 1-bit controlling signal ( $V_{\text{CTRL}}$ ) divides the output of CM into two values. 1 and 0 of  $V_{\text{CTRL}}$  result in high and low bias currents, respectively. Since the required minimum of bias current is above zero,  $R_{\text{P}}$  was utilized as the determination of minimum output current of the CM.

The stability of the BJT should be examined before deciding the range of the bias current. The  $\mu$  criterion was utilized to examine the stability. Figure 9 shows the curve of  $\mu$ value versus bias current. It is obvious that the LNA is stable ( $\mu > 1$ ) when bias current is greater than 1.5 mA. Considering the required NF, IIP3 and convenience of network matching, the range of bias current is set from 1.5 to 13 mA.



Fig. 11. Measurement and simulation results of LNA: (a) NF versus bias current; (b) IIP3 versus bias current.

Table 1. Comparison of LNAs' performance.

|                      | Freq.    | Gain | IIP3  | NF   |
|----------------------|----------|------|-------|------|
|                      | (MHz)    | (dB) | (dBm) | (dB) |
| This work            | 860      | 9    | 19.83 | 1.47 |
| Bias current at 5 mA | 860      | 9.1  | 8.51  | 1.62 |
| Ref. [10]            | 800-2100 | 14.5 | 16    | 2.6  |
| Ref. [11]            | 869-896  | 16.2 | 8     | 1.2  |
| Ref. [12]            | 900      | 17   | -5.1  | 3.4  |

Then the performance of the CM is investigated. Figure 10(a) gives simulation results, including the waveform of the  $V_{\text{CTRL}}$  and  $I_{\text{OUT}}$ . Figure 10(b) gives the measurement result where the voltage of  $R_{\text{OUT}}$  ( $V_{\text{OUT}}$ ) is tested. Since  $I_{\text{OUT}}$  flows through the  $R_{\text{OUT}}$ ,  $V_{\text{OUT}}$  can represent  $I_{\text{OUT}}$ . It is due to the parasitic capacitance that there is a little while between shifting edges of  $V_{\text{CTRL}}$  and  $I_{\text{OUT}}$ .  $I_{\text{OUT}}$  becomes steady in 5  $\mu$ s after  $V_{\text{CTRL}}$  changes and the steady low and high values of the  $I_{\text{OUT}}$  meet the design specifications.

The NF and IIP3 of the LNA are measured. Figure 11 gives the NF and IIP3 values of the LNA.

In contrast, another experiment where the LNA's bias current was set still to 5 mA was also performed. Table 1 gives performance comparison between these two experiment and some other LNAs reported recently.

According to the measurement results, the LNA with tunable bias current satisfy the required specifications. Compared with an LNA with a constant bias current (5 mA), this adjustable LNA has obvious advantages, e.g. the NF is improved by 0.15 dB and IIP3 is increased by 11.32 dB.

#### 5. Conclusion

The CM circuits proposed in this paper have tunable output current. There are two ways to tune the current. While one method utilizes an analog voltage source which has an almost linear relationship with the output current, the other one makes use of an *N*-bit digital signal input which divides the output current into  $2^N$  values. The CM has the advantages of simplicity and convenience in use.

The tunable CM has been applied as the bias current of the LNA in a wireless receiver. As the bias current is tunable, the LNA can achieve a lower NF and a higher IIP3 than a conventional one. Then a larger dynamic range is achieved with the method of tuning the bias current according to the strength of the received signal.

The experimental results of the CM and LNA are both very consistent with the theoretical analysis.

# References

- Hamed H F A, Kaya S. Low voltage programmable double-gate MOSFETs current mirror and its application as programmablegain current amplifier. 14th IEEE International Conference on Electronics, Circuits and Systems, 2007, 1–4: 391
- [2] Souliotis G, Psychalinos C. Current-mode linear transformation filters using current mirrors. IEEE Trans Circuits Syst II, 2008, 55(6): 541
- [3] Somdunyakanok M, Pattanathadapong T, Prommee P. Accurate tunable current-mirror and its applications. International Symposium on Communication and Information Technologies, 2008: 56
- [4] Yang B D, Kim J S, Yun J K, et al. A highly accurate BiC-MOS cascode current mirror for wide output voltage range. Proceedings of IEEE International Symposium on Circuits and Systems, 2008, 1–10: 2314
- [5] Guvenc U, Zeki A. Tunable linear current mirror. Proceedings of PhD Research in Microelectronics and Electronics, 2008: 49
- [6] Lerdworatawee J, Namgoong W. Revisiting spurious-free dynamic range of communication receivers. IEEE Trans Circuits Syst I, 2006, 53(4): 937
- [7] Helmy A, Sharaf K, Ragai H. On the SFDR performance of BJT RF circuits, an analytical approach. Proceedings of the 12th International Conference on Microelectronics, 2000: 375
- [8] Kim S H, Okada M, Hara T, et al. Study on the adaptive RF front-end for low power consumption ISDB-T receiver. IEEE Military Communications Conference, 2007, 1–8: 2775
- [9] Ding Y, Harjani R. A +18 dBm IIP3 LNA in 0.35 μm CMOS. IEEE Int Solid-State Circuits Conf Tech Dig, 2001: 162
- [10] Chen W H, Liu G, Zdravko B, et al. A highly linear broadband CMOS LNA employing noise and distortion cancellation. IEEE J Solid-State Circuits, 2008, 43(5): 1164
- [11] Kim N, Aparin V, Barnett K, et al. A cellular-band CDMA 0.25μm CMOS LNA linearized using active post-distortion. IEEE J Solid-State Circuits, 2006, 41(7): 1530
- [12] Xin C Y, Sanchez-Sinencio E. A GSM LNA using mutualcoupled degeneration. IEEE Microw Wireless Compon Lett, 2005, 15(2): 68