Stacking fault energy in some single crystals

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Abstract: The stacking fault energy of single crystals has been reported using the peak shift method. Presently studied all single crystals are grown by using a direct vapor transport (DVT) technique in the laboratory. The structural characterizations of these crystals are made by XRD. Considerable variations are shown in deformation (α) and growth (β) probabilities in single crystals due to off-stoichiometry, which possesses the stacking fault in the single crystal.

Key words: single crystals; X-ray diffrectograms; deformation probability; growth probability; stacking fault **DOI:** 10.1088/1674-4926/33/6/062001 **EEACC:** 2520

1. Introduction

A basic understanding of the deformation characteristics and mechanical behavior of materials requires the knowledge of the stacking-fault energy (SFE). This aspect is relevant because various mechanical properties such as strength, toughness and fracture are severely affected by stacking-fault energy (SFE) due to its direct influence on the slip mode, deformation twinning and martensitic transformations. Thus, in alloy design, it is important to understand how stacking-fault energy (SFE) is affected by composition. Lamellar solids of transition metal dichalcogenides (TMDC) MX_2 (M = Mo, W, Nb, Ta and X = S, Se, Te) have been extensively studied because of their excellent lubricating properties and photovoltaic behavior. These materials, being semiconducting and of a layered structure, may undergo structural and electronic transitions under pressure. They typically have a hexagonal structure, which is composed of two-dimensional sheets stacked on top of one another. Each sheet is tri-layered with a metal atom in the middle that is covalently bonded to chalcogen atoms in the top and bottom layers. The covalently bonded sheets are held together by weak van der Waals forces, which permit them to shear easily. At high pressures the fluid lubricants squeeze out from in-contact surfaces, causing high friction and wear. With lamellar solids such as TMDCs, shearing takes place more easily when loads are high. Hence, lamellar solids are well-suited to extreme pressure lubrication. Structural transitions and metallization are of relevance in its application as lubricant. These crystals become superconducting when intercalated with alkali and alkaline earth metals^[1-19]. The study of stacking faults is very important one, because it plays an important role in the description of defects. The conversion behaviour of a solar cell is closely related to the perfection of the electrode material and since stacking faults play a fundamental role in the description of structural defects, their study is of both practical and theoretical interest. The enhanced conduction of the stacking fault along the *c*-axis is difficult to understand because of the extreme 2D characters of the layered

compounds of MoSe₂. The only way to understand this conduction is by supposing the presence of stacking faults in these crystals. We have reported some structural, electric and optical properties of TMDC materials^[1-15] briefly. Very recently, Sumesh *et al.*^[16, 17] have reported specific contact resistance at In-nMoSe₂ interfaces and current–voltage–temperature characteristics experimentally. The stacking fault energy of various compounds has been studied by various researchers^[18–31]. It is clear from the literature survey that research on the stacking fault energy of the various intercalated and doping compounds of MoSe₂ is almost negligible. Hence, in the present article, we have decided to work on intercalated In_xMoSe₂ (0 $\leq x \leq$ 1) and doped MoRe_{0.005}Se_{1.995}, MoRe_{0.001}Se_{1.999} and Mo_{0.995}Re_{0.005}Se₂ single crystals.

2. Experimental methodology

All of the studied single crystals were grown by using the direct vapor transport (DVT) method inside a dual zone horizontal furnace^[1-15]. In the present case, a furnace controlled by a micro controller with thermal profile programming facilities and a solid state relay (SSR) based power unit for the two zones of the furnace with suitable back up to take care of power supply breakups has been used. A high quality fused quartz tube is used for crystal growth.

The formation and occurrence of crystal imperfections known as stacking faults is important to the mechanisms and models postulated to explain work hardening and recovery of closely packed metals and alloys. Stacking faults represent disorders in stacking atomic planes which are formed during the process of crystal growth, plastic deformation, phase transformations and by the condensation and collapse of vacancy discs. In a face centered cubic (FCC) structure, the stacking fault is a thin slab with a hexagonal closely packed (HCP) structure and in HCP materials the stacking fault is a thin layer with an FCC structure. The faults are formed when disorders in stacking the closely packed layers occur. The TMDC compounds have the general formula TX₂, where T is a transition metal from IV-B, V-B and the VI-B group of the periodic table and

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Fig. 1. X-ray diffractograms of In_{0.25}MoSe₂.



Fig. 2. X-ray diffractograms of In_{0.50}MoSe₂.



Fig. 3. X-ray diffractograms of In_{0.75}MoSe₂.



Fig. 4. X-ray diffractograms of InMoSe2.



Fig. 5. X-ray diffractograms of MoRe_{0.005}Se_{1.995} single crystal.



Fig. 6. X-ray diffractograms of MoRe_{0.001}Se_{1.999} single crystal.

X is one of the chalcogens sulfur, selenium or tellurium. The basic structure of loosely coupled X–T–X sheets makes such materials extremely interesting such that, within a layer, the bonds are strong, while between the layers they are remarkably weak. Basically, the stacking faults in the single crystals are detected by using X-rays. With a view to examining the proposed correlation between stacking faults and the deformation-induced structural transformation, the stacking fault probabil-

ity in presently taken single crystals has been determined by X-ray diffraction methods. In the present study all of the single crystals are found to be HCP type in nature.

The X-ray diffractogram was recorded using a Philips Xray diffractometer using CuK α radiation. For this purpose, many small crystals from each group were finely ground using an agate mortar and filtered through a 106- μ m sieve to obtain grains of nearly equal size. The X-ray diffractograms of

hkl value	MoRe _{0.005} Se _{1.995}			MoRe _{0.001} Se _{1.999}			Mo _{0.995} Re _{0.005} Se ₂		
	<i>d</i> -value (Å)	Peak in- tensity count $(\beta_{2\theta})$ (s^{-1})	Angle (2θ) (Å)	<i>d</i> -value (Å)	Peak in- tensity count $(\beta_{2\theta})$ (s^{-1})	Angle (2θ) (Å)	<i>d</i> -value (Å)	Peak in- tensity count $(\beta_{2\theta})$ (s^{-1})	Angle (2θ) (Å)
102	2.6158	0.080	34.255	2.6111	0.140	34.315	2.6082	0.080	34.395
103	2.3774	0.060	37.810	2.3756	0.080	37.840	2.3756	0.120	37.840
105	1.9152	0.100	47.430	1.9112	0.080	47.535	1.9147	0.080	47.445

Table 1. Structural parameters used in the calculation of stacking fault energy for Re-doped single crystals.

Table 2. Structural parameters used in the calculation of stacking fault energy for $In_x MoSe_2$ ($0 \le x \le 1$) single crystals.

hkl voluo	In _{0.25} MoSe ₂			In _{0.50} MoSe ₂		In _{0.75} MoSe ₂				InMoSe ₂		
nki value	d -	Peak	Angle	<i>d</i> -	Peak	Angle	<i>d</i> -	Peak	Angle	<i>d</i> -	Peak	Angle
	value	inten-	(2θ)	value	inten-	(2θ)	value	inten-	(2θ)	value	inten-	(2θ)
	(Å)	sity	(Å)	(Å)	sity	(Å)	(Å)	sity	(Å)	(Å)	sity	(Å)
		count			count			count			count	
		$(\beta_{2\theta})$			$(\beta_{2\theta})$			$(\beta_{2\theta})$			$(\beta_{2\theta})$	
		(s^{-1})			(s^{-1})			(s^{-1})			(s^{-1})	
102	2.6158	0.080	34.255	2.6111	0.140	34.315	2.6082	0.080	34.395	2.6097	0.240	34.335
103	2.3774	0.060	37.810	2.3756	0.080	37.840	2.3756	0.120	37.840	2.3774	0.080	37.810
105	1.9152	0.100	47.430	1.9112	0.080	47.535	1.9147	0.080	47.445	1.9171	0.080	47.380

Table 3. Stacking fault probabilities of $In_x MoSe_2$ ($0 \le x \le 1$) single crystals.

Stacking fault probability	In _{0.25} MoSe ₂	In _{0.50} MoSe ₂	In _{0.75} MoSe ₂	InMoSe ₂
α	0.0025037	0.0026711	0.0023574	0.0033694
β	0.0025299	0.0027837	0.0022524	0.0032857

Table 4. Stacking fault probabilities of Re-doped MoSe₂ single crystals.

Stacking fault probability	MoRe _{0.005} Se _{1.995}	MoRe _{0.001} Se _{1.999}	Mo _{0.995} Re _{0.005} Se ₂
α	0.0025037	0.0026711	0.0023574
β	0.0024799	0.0026637	0.0023324



Fig. 7. X-ray diffractograms of Mo_{0.995}Re_{0.005}Se₂ single crystal.

all the single crystals are displayed in Fig. 1–7. The structural parameters used in the calculation of the stacking fault energy (SFE) taken from the X-ray diffractograms of the single crystals are tabulated in Tables 1 and 2, which are used in present calculation.

The stacking fault probabilities of the samples were measured by using peak shift methods. According to Warren's Xray diffraction theory^[18], the diffraction peak shift is due to the deformation fault in the HCP crystal. Hence, such probability can be determined by measuring the peak shift. For that, the formulas of deformation and growth probabilities given by Warren^[18] are as follows

$$B_{2\theta} = \frac{360 \tan \theta}{\pi^2} l \left(\frac{d}{c}\right)^2 (3\alpha + 3\beta), \quad l \text{ even}, \qquad (1)$$

and

$$B_{2\theta} = \frac{360 \tan \theta}{\pi^2} l \left(\frac{d}{c}\right)^2 (3\alpha + \beta), \quad l \text{ odd}, \qquad (2)$$

where $B_{2\theta}$ denotes the full width at half the maximum intensity, *d* is the *hkl* spacing, *c* is equal to $2d_{002}$, and α and β are the deformation fault probability and the growth probability. Values of the deformation fault probability α and the growth probability β have been estimated from the observed peak shifts and the peak asymmetry, respectively. The presently calculated values of α and β are shown in Tables 3 and 4. All the calculations are performed for (102), (103) and (105) reflections. The peak displacement due to faults in the HCP structure is usually very small and therefore, it is in general advisable to try measuring a pair of close reflections.

3. Results and discussion

From studies of Tables 3 and 4, it is seen that there is a significant variation shown in the deformation fault probability (α) and growth probability (β) due to off-stoichiometry i.e. composition of indium in the MoSe₂ and Re-doped MoSe₂ viz. MoRe_{0.005}Se_{1.995}, MoRe_{0.001}Se_{1.999} and Mo_{0.995}Re_{0.005}Se₂ single crystals. The variation of stacking fault i.e. both probabilities is due to the creation of the defects in the crystal. The values of α and β are seen nearly of the same order. Any theoretical or experimental proof of such types of calculation is not available in the literature so it is difficult to compare our results with them and make any strong remarks. The calculation of the stacking fault may be considered as one of the guidelines for further detailed study of defects and various properties of crystals.

It was shown by Cockyne et al.^[19] that significant improvement in resolution of the structure of lattice defects could be obtained from dark field electron micrographs taken in weakly diffracted beams. Ray and Cockyne^[20] have used the weak beam technique for directly observing the splitting of dislocations into partials of Si. Since then, several investigators^[21-25], most recently Mao and Knowles^[26], have observed the dissociation of lattice dislocations into partials. The presence of stacking faults has been studied by Agarwal et al. [27, 28] in WS2. WS1.8 and WSe2 single crystals. All these investigators have used the spacing between partials to estimate the stacking fault energy (SFE) in the crystal compounds. Gross and Teichler^[29] have formulated a real space method, Kenway^[30] has adopted an atomic lattice stimulation and Xiliang et al.^[31] have used a method based on an improved embeddedatom method for theoretical estimation of stacking fault energies in different materials. All these estimations when compared with stacking fault energy measurements made using weak beam techniques show a favourable agreement.

The low values of stacking fault probabilities allows for easy gliding on the basal plane of $In_x MoSe_2$ ($0 \le x \le 1$) and Re-doped MoSe₂ viz. MoRe_{0.005}Se_{1.995}, MoRe_{0.001}Se_{1.999} and Mo_{0.995}Re_{0.005}Se₂ layers thus leading to easy creation of stacking faults and its excellent properties as solid lubricating agent. The above results indicate that the peak-shift method described in the present work has been successfully developed for the determination of deformation fault probability (α) and growth probability (β).

4. Conclusion

X-ray diffractogrms have clearly shown that the difference in the presently studied single crystals is due to offstoichiometry. The analysis of the deformation fault probability (α) and growth probability (β) of all the single crystals has shown that indium intercalation and Re-doping affect the stacking fault probabilities. The experimental proof is not available in the literature, but the present investigation provides an important set of data for most of the single crystals, which can be very useful for further comparison either with theory or experiment. A study on the stacking fault of other single crystals is in progress.

References

- [1] Vora A M, Garg P K. Effect of indium intercalation on various properties of $In_x MoSe_2$ ($0 \le x \le 1$) single crystals. Indian J Phys, 2000, 74A: 563
- [2] Vora A M. Transport properties measurement of indium intercalated molybdenum Diselenide single crystal. M Phil Dissertation, Sardar Patel University, Vallabh Vidyanagar, India, 1998
- [3] Vora M M, Vora A M. Anisotropy of the optical absorption in layered single crystals. Cryst Res Tech, 2006, 41: 803
- [4] Vora M M, Vora A M. Anisotropy of the optical absorption in layered single crystals of MoRe_{0.001}Se_{1.999}. Cryst Res Tech, 2007, 42: 50
- [5] Vora M M, Vora A M. Intercalation and anisotropy of optical absorption of MoRe_{0.005}Se_{1.995} single crystal. Cryst Res Tech, 2007, 42: 186
- [6] Vora A M. Effect of indium intercalation on various properties of MoSe₂ single crystals. Cryst Res Tech, 2007, 42: 286
- [7] Vora M M, Vora A M. Electrical properties measurements of Re doped MoSe₂ single crystals. The African Phys Rev, 2011, 6: 129
- [8] Vora M M, Vora A M. Electrical properties measurements of In_xMoSe₂ (0 ≤ x ≤ 1) single crystal. Chalcogenide Lett, 2007, 4: 77
- [9] Vora M M, Vora A M. Intrinsic stacking fault in single crystal of In_xMoSe₂ (0 ≤ x ≤ 1). Chalcogenide Lett, 2007, 4: 85
- [10] Vora M M, Vora A M. Effect of rhenium doping on various properties of MoSe₂ single crystal. Chalcogenide Lett, 2007, 4: 97
- [11] Vora A M. Effect of rhenium doping on various properties of MoRe_{0.001}Se_{1.999} single crystal. Chalcogenide Lett, 2008, 5: 17
- [12] Vora M M, Vora A M. Stacking faults in Re doped MoSe₂ single crystals. Chalcogenide Lett, 2008, 5: 35
- [13] Vora M M, Vora A M. Effect of rhenium doping on various physical properties of single crystals of MoSe₂. Chalcogenide Lett, 2008, 5: 65
- [14] Vora M M, Vora A M. Stacking faults in the single crystals. Semicond Phys Quant Ele Opto Ele, 2009, 12: 421
- [15] Vora A M. Stacking faults in the single crystals. J Electron Device, 2011, 12: 734
- [16] Sumesh C K, Patel K D, Pathak V M, et al. Specific contact resistance at In-nMoSe₂ interfaces. J Electron Device, 2010, 8: 324
- [17] Sumesh C K, Patel K D, Pathak V M, et al. Analysis of current-voltage-temperature characteristics of In and Cu contacts on n-type MoSe₂ single crystals. Cryst Res Technol, 2011, 46: 61
- [18] Warren B E. X-ray studies of deformed metals. Prog Met Phys, 1959, 8: 147
- [19] Cockayne D J H, Ray I L F, Whelan M J. Investigations of dislocation strain fields using weak beams. Phil Mag, 1969, 20: 1265
- [20] Ray I L F, Cockayne D J H. The dissociation of dislocations in silicon. Proc Roy Soc London, 1971, A325: 543
- [21] Stenkamp D, Jager W. Dislocations and their dissociation in Si_xGe_{1-x} alloys. Phil Mag, 1992, A65: 1369
- [22] Mckernain S, Zhu G J, Carter C B. Observation of double ribbons in GaAs and AlGaAs. Phil Mag Lett, 1991, 64: 349
- [23] Cosandey F, Plano R. Determination of stacking fault energies of Ni–Cr–Ce alloys. Scr Metall Mater, 1992, 26: 723
- [24] Suzuki K, Ichihara M, Takeuchi S. High-resolution electron microscopy of extended defects in wurtzite crystals. Jpn J Appl Phys, 1994, 33: 1114
- [25] Yau J K, Munroe P R, Sorrell C C. Young's modulus and stacking-fault energy of the (Bi, Pb)₂Sr₂Ca₂Cu₃O_{10 + x} super-

conductor. Physica C, 1995, 243: 359

- [26] Mao Z, Knowles K M. Dissociation of lattice dislocations in Sr-TiO₃. Phil Mag, 1996, A73: 699
- [27] Agarwal M K, Patel Y, Vashi M N. Stacking faults in WS₂ and WS_{1.8} single crystals. Indian J Pure & Appl Phys, 1999, 37: 464
- [28] Agarwal M K, Patel J V, Patel N G. Stacking fault energy measurements in WSe₂ single crystals using weak-beam techniques. Phys Status Solidi A, 1981, 66: 425
- [29] Gross A, Teichler H. Real-space method for total-energy calculations in semiconductors: estimation of stacking fault energies. Phil Mag, 1991, B64: 413
- [30] Kenway P R. Calculated stacking-fault energies in α-Al₂O₃. Phil Mag, 1993, B68: 171
- [31] Nie X, Wang R, Ye Y, et al. Calculations of stacking fault energy for fcc metals and their alloys based on an improved embeddedatom method. Solid State Commun, 1995, 96: 729